

# IMECC NA2

Development of a Network Design Tool

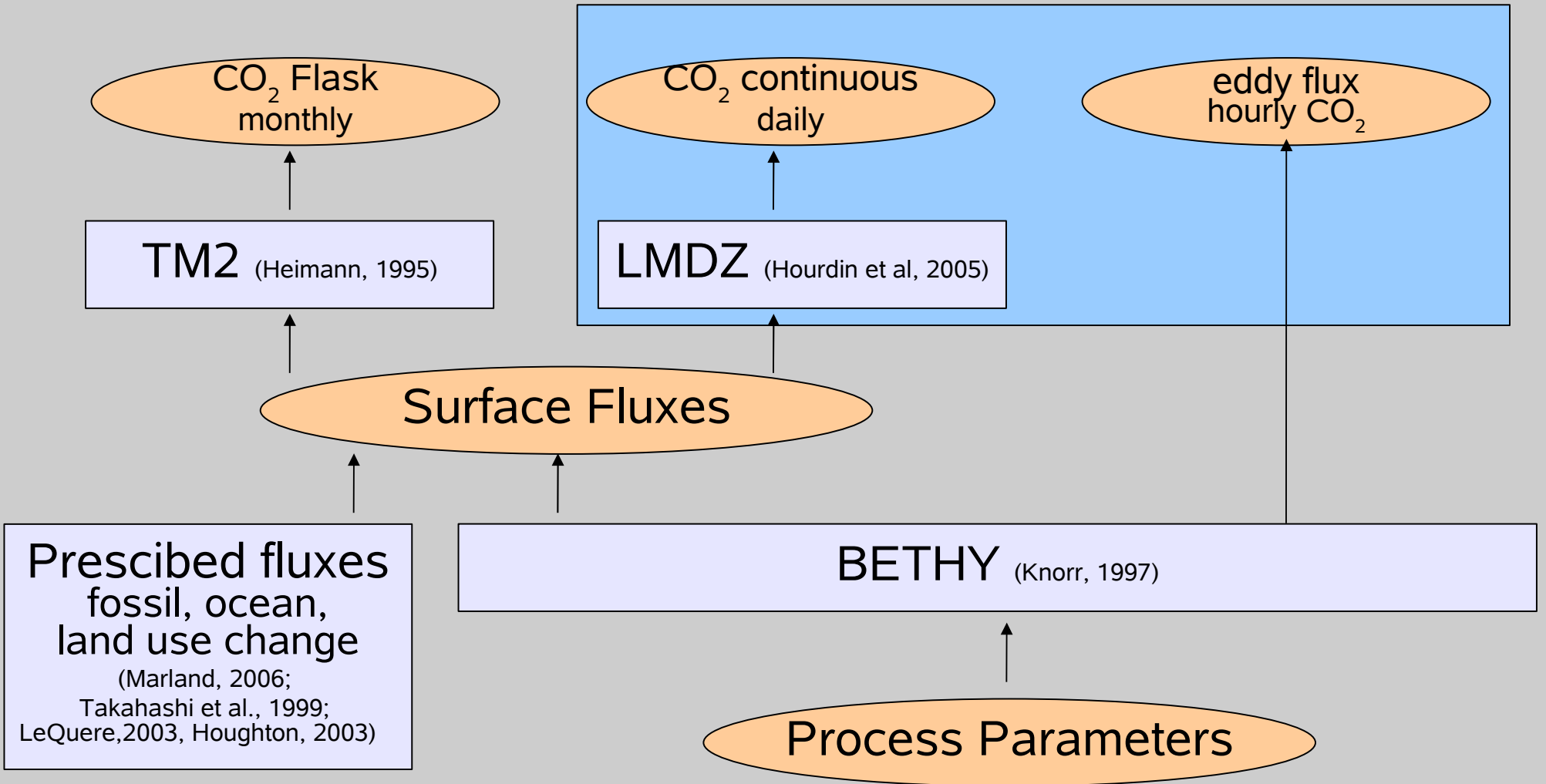
FastOpt, LSCE, and University of Bristol

GEOMON & IMECC Meeting, January 2009, Geneva

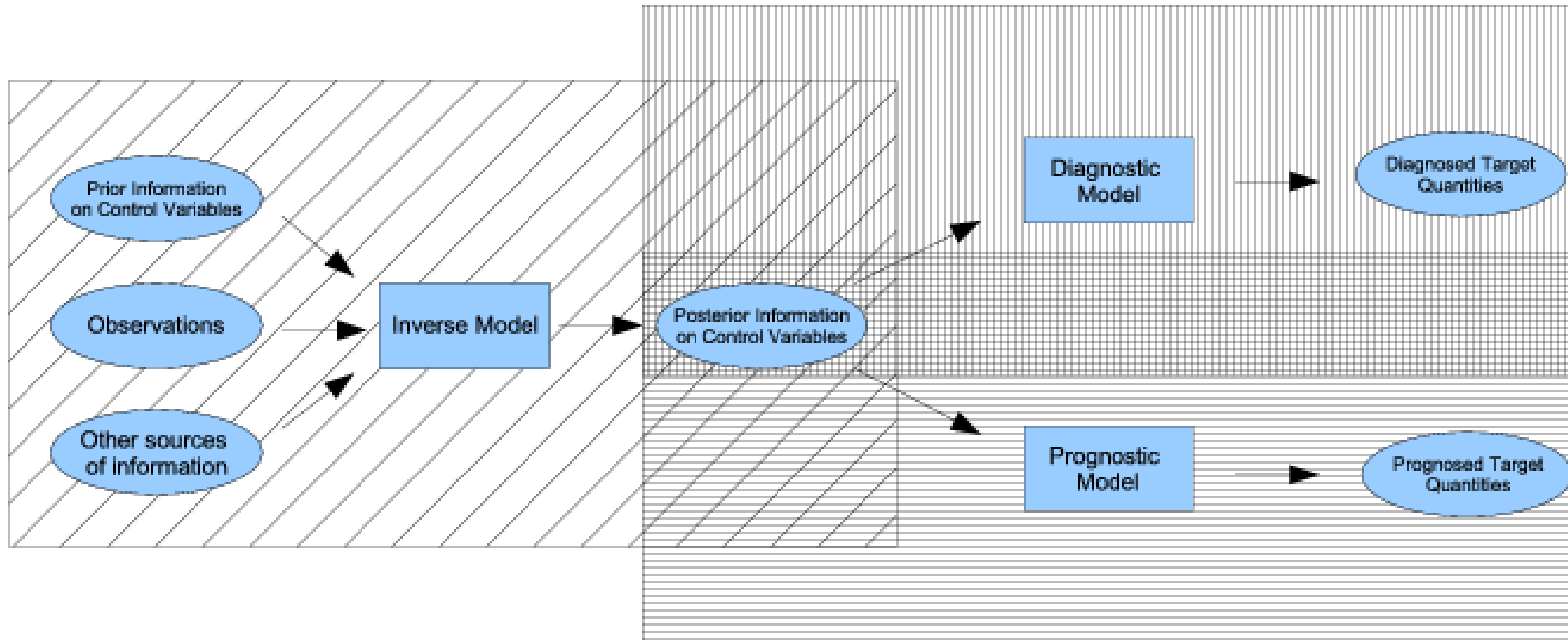


**FastOpt**

# Carbon Cycle Data Assimilation System (CCDAS) Forward Modelling Chain



# CCDAS scheme



Rayner et al. (2005); Scholze et al. (2007)

# Uncertainty calculation in 2 steps

Inverse step:

$$J(x) = \frac{1}{2} (x - x_{pr})^T C_{pr}^{-1} (x - x_{pr}) + \frac{1}{2} \sum_{i=1,nd} \left( \frac{M_i(x) - d_i}{\sigma_{d_i}} \right)^2$$

$$\frac{d^2 J(x)}{dx^2} = C_{pr}^{-1} + \sum_{i=1,nd} \frac{1}{\sigma_{d_i}^2} \frac{d^2}{dx^2} (M_i(x) - d_i)^2$$

- Hessian independent of  $x$  for linear model
- For synthetic data use  $d = M(x)$ .
- Decomposes nicely, can precompute model contribution

uncertainty  
in observations  
AND model

$$C_{po} \approx \frac{d^2 J(x_{po})}{dx^2}^{-1}$$

Propagation step:

$$\sigma_y^2 \approx \frac{dy(x_{po})}{dx} C_{po} \frac{dy(x_{po})}{dx}^T \approx \frac{dy(x_{po})}{dx} \frac{d^2 J(x_{po})}{dx^2}^{-1} \frac{dy(x_{po})}{dx}^T$$

$x$ : Parameters  
 $x_{pr}$ : Priors  
 $C_{pr}$ : Uncertainties  
 $M(x)$ : Model  
 $d$ : Observations  
 $C_d$ : Their uncertainties  
 $\sigma_{d_i}$ : Uncorrelated!  
 $J(x)$ : Cost function  
 $\frac{d^2 J(x)}{dx^2}$ : Hessian  
 $x_{po}$ : Posterior parameters  
 $C_{po}$ : Posterior uncertainties  
 $y(x)$ : Target quantity  
 $\sigma_y$ : Its uncertainty

All derivative code  
 generated from model code  
 by automatic differentiation  
 tool TAF